Molecular Cell
Creating Single-Copy Genetic Circuits

Graphical Abstract

Highlights

- Reduced transcription leakage improves toggle robustness to parameter variation/noise
- Mathematic models identify important design parameters that affect circuit stability
- Empirical strategies for single-copy circuit construction are reported
- Genome-integrated circuit places minimal metabolic burden on the host cell

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In Brief
Lee et al. (2016) use theoretical and empirical design and analysis to build a bistable, genome-integrated genetic toggle switch with reduced growth burden on the host cell. They demonstrate that reduced transcriptional leakage improves the robustness of the circuit to parameter variation and noise.

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Creating Single-Copy Genetic Circuits

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SUMMARY

Synthetic biology is increasingly used to develop sophisticated living devices for basic and applied research. Many of these genetic devices are engineered using multi-copy plasmids, but as the field progresses from proof-of-principle demonstrations to practical applications, it is important to develop single-copy synthetic modules that minimize consumption of cellular resources and can be stably maintained as genomic integrants. Here we use empirical design, mathematical modeling, and iterative construction and testing to build single-copy, bistable toggle switches with improved performance and reduced metabolic load that can be stably integrated into the host genome. Deterministic and stochastic models led us to focus on basal transcription to optimize circuit performance and helped to explain the resulting circuit robustness across a large range of component expression levels. The design parameters developed here provide important guidance for future efforts to convert functional multi-copy gene circuits into optimized single-copy circuits for practical, real-world use.

INTRODUCTION

Multi-copy plasmids are the workhorses of genetic engineering and are commonly used by both microbes in the environment and biologists in the lab to express and exchange genetic information. Microbes use plasmids to acquire genetic components including virulence factors and antibiotic resistance cassettes that provide an evolutionary advantage in a particular environmental niche (Davies and Davies, 2010; Norman et al., 2009). These plasmids serve as a common vehicle for horizontal gene transfer to surrounding microbes, but genetic components that are particularly useful are often integrated into the genome to increase their stability and reduce the metabolic burden of plasmid maintenance (Bergstrom et al., 2000; Davison, 1999; Ochman et al., 2000; Rankin et al., 2011). In a broadly similar approach, basic and applied biologists rely on multi-copy plasmids to construct and test genetic components for a wide range of applications, from simple gene expression in a target organism to complex gene circuit design for industrial or therapeutic use. Synthetic biologists and metabolic engineers commonly use an iterative “design-build-test” approach that relies on the ease of multi-copy plasmid construction and purification to generate complex genetic circuits (Cameron et al., 2014; Keasling, 1999; Khalil and Collins, 2010; Lee et al., 2012). As these applied-biology fields progress from proof-of-principle demonstrations to practical applications, however, these circuits must also be converted into single-copy synthetic modules that minimize resource consumption and can be stably integrated into the genome to minimize the possibility of horizontal gene transfer.

As both natural and applied systems must transfer genetic elements from multi-copy plasmids to single-copy genomic integrants, it is important to understand the design parameters that enable proper regulation and expression of these genetic components during this process. In this study, we use the conversion of a multi-copy genetic toggle switch to an optimized single-copy circuit as a case study to examine the design principles that affect circuit performance. We use empirical design and iterative construction and testing to build a bistable, genome-integrated toggle switch with reduced growth burden. To identify regulatory elements that are important for circuit function, we test a series of control mechanisms including promoter-level transcriptional control (repressor binding strength and operator site location and number), posttranscriptional control (5’ untranslated region [UTR]), and translational control (ribosome binding site [RBS] strength). In parallel to this empirical approach, we use deterministic and stochastic models to identify important design parameters that affect circuit function and stability, and we use these models to explain the robustness of the optimized toggle switch to translation-based perturbations. Finally, to demonstrate the practical application of the optimized circuit, we use the single-copy toggle switch to build a genome-integrated “kill switch” that provides exogenous control of cell...
viability with minimal metabolic load that is highly stable. This case study, and the design parameters that we identify, offer fundamental guidance for future efforts to convert multi-copy gene circuits into functional single-copy circuits and provide a window into the intricate adaptations that microbes must make as they incorporate plasmid-borne genes into their genome.

RESULTS AND DISCUSSION

Conversion of the Multi-Copy Toggle Switch to Single-Copy

To identify the design parameters important for single-copy genetic circuit conversion, we chose to study a multi-copy genetic toggle switch that uses reciprocal regulation of the transcriptional repressors LacI and TetR to generate a bistable system (Cameron and Collins, 2014; Gardner et al., 2000; Kobayashi et al., 2004; Litcofsky et al., 2012) (Figure 1A). The toggle remains in its designated state in the absence of any exogenous input but can be switched to the opposite state with the small molecule inducers anhydrotetracycline (ATc) or isopropyl β-D-1-thiogalactopyranoside (IPTG), which regulate TetR and LacI, respectively. To clearly identify each toggle state in the single-copy circuit, we first modified the RBS of both the GFP and mCherry reporters to increase their induced expression levels (Figure 1B and see Figure S1 available online). Using control cells to define the fluorescence threshold for each toggle state (Figure S1), we quantified circuit stability in both the LacI+ and the TetR+ states and found that the circuit was only stable in the TetR+ state (red state) (Figure 1C). Upon removal of the ATc used to induce the LacI+ state (green state), LacI repression of TetR and mCherry diminished rapidly, allowing TetR to quickly repress LacI and GFP to switch the toggle state back to the TetR+ state (Figure 1C). Earlier work by Ying et al. to create a single-copy toggle switch also resulted in circuit monostability in the absence of chemical inducers (Ying et al., 2010), further demonstrating the need for specific design principles to produce functional, single-copy synthetic circuits.

Mathematical Modeling to Recover Toggle Switch Bistability

To better understand single-copy toggle switches and recover circuit bistability, we developed a mechanistic model of toggle switch dynamics (see Experimental Procedures).
and Supplemental Procedures 1 and 2). This model is derived from a biochemical rate equation formulation of gene expression with parameters including the plasmid copy number $n$, the dissociation constants $k$ of the repressors to their respective promoters, the lumped constant $\alpha$ encompassing the transcription and translation rate constants, the decay rate constant $\delta$ of the repressors, and $\varepsilon$ characterizing the leakage of the promoters ($\varepsilon = 0$ when the promoter is tightly repressed, and $\varepsilon = 1$ if the promoter is not repressed at all by its repressor) (see Experimental Procedures and Supplemental Procedures 1 and 2). In this model, the equilibria of the toggle switch can be characterized in a high-dimensional parameter space using only numerical methods, and as a result, this approach provides little guidance to recover bistability (see Supplemental Procedures 3). To enable the analytical characterization of bistability, we constrained the model to symmetric toggle switches, thereby limiting the parameter space to three dimensions $(k, \mu, \varepsilon)$, where $\mu = n\alpha/\delta$ is the steady-state concentration of the unpressed proteins (see Supplemental Procedures 3). In particular, the toggle switch is bistable if and only if

$$\mu^2 k^2 (1 - \varepsilon)^2 - 4k(k + \mu \varepsilon)(k + \varepsilon^2 \mu^2) > 0.$$ 

Further analysis yields that the above condition holds true if and only if the leakage $\varepsilon$ is smaller than the critical threshold $\varepsilon^*$, plotted in Figure 1D (the expression of $\varepsilon^*$ is given in Supplemental Procedures 3). The value of $\mu$ decreases with plasmid copy number in this model, reshaping the region of bistability to render the single-copy toggle switch monostable (Figures 1D–1F, detailed in Supplemental Procedures 4). As a result, while the pair $(k, \varepsilon)$ lies in the region of bistability for the multi-copy toggle (Figure 1E), it lies outside in the single-copy case (Figure 1F). Furthermore, the model predicts that bistability can be recovered by increasing TetR and LacI expression to restore $\mu$ to its original value and by decreasing the promoter leakage $\varepsilon$ (see Supplemental Procedures 4).

Rebalanced Regulator Expression in the Single-Copy Toggle

To enhance LacI and TetR expression on the single-copy plasmid, we mutagenized the RBS for each gene and used C-terminal mCherry fusions to LacI and TetR to measure their expression. This approach enabled us to bring induced TetR expression levels up to that seen in the multi-copy plasmid (Figure 2A and Supplemental Procedures 5), but additional mutagenesis of the LacI promoter and 5’ UTR was required to achieve LacI expression levels equivalent to the multi-copy plasmid (Figures 2B and Supplemental Procedures 5). To determine if increased LacI and TetR expression and the resulting restoration of $\mu$ in our mechanistic model were sufficient to recreate the bistability seen in the multi-copy plasmid, several combinations of LacI and TetR expression variants were tested on the single-copy plasmid. A majority of the circuits remained monostable in the red state, and the high LacI expression variant (L5-T3) shifted the monostability to the green state, but none of the combinations displayed the desired bistability (Figures 2C and 2D; Table S1). In particular, the LacI and TetR expression variants that most closely recapitulated the multi-copy expression level (L5-T3) did not produce a bistable circuit (Figure 2E).
Tightened Transcriptional Repression to Recover Circuit Bistability

Our mechanistic model of the circuit predicts that reduced leakage $\varepsilon$ will increase toggle switch bistability, yielding greater robustness to parameter variations (Supplemental Procedures 6), and a complementary stochastic model of circuit function similarly predicts that tight transcriptional control plays a fundamental role in providing robustness to noise in single-copy circuits (Supplemental Procedures 7). We therefore focused our attention on reducing the basal expression of LacI and TetR in their repressed state. We first sought to minimize leaky transcription from the $P_{Trc2}$ promoter driving TetR expression, since unwanted TetR expression was the likely cause of LacI+/GFP+ instability in nearly all of the single-copy toggle variants. Mutations in LacI that increase affinity to its native $O_1$ operator site did not improve toggle bistability (Figure S3), so we next sought to reduce basal transcription by replacing the $O_1$ operator site with the palindromic operator site $O_{id}$ that binds LacI more strongly (Sadler et al., 1983)(Figure 3A). As seen in Figure 3B, real-time PCR (RT-qPCR) analysis of tetR transcription showed that the $O_{id}$ operator significantly lowered basal tetR transcription, and inclusion of additional $O_{id}$ sites upstream of the $P_{Trc2}$ $-35$ element caused a further reduction in tetR mRNA levels. To determine if the lowered tetR mRNA levels would affect circuit stability, we cloned the improved promoters $P_{T2}$, $P_{T3}$, and $P_{T4}$ into the $L_e$-$T_4$ single-copy toggle and measured circuit bistability. As seen in Figure 3C, toggles containing $P_{T2}$, $P_{T3}$, and $P_{T4}$ promoters displayed strong bistability for over 72 hr. As $P_{T4}$ provided equivalent stability to $P_{T3}$, we chose $P_{T3}$ for continued circuit development.

With the clear role of transcriptional leakage $\varepsilon$ in toggle bistability, we re-examined the range of LacI and TetR expression levels that maintain bistability in single-copy toggles with low promoter leakage. In contrast to toggle variants containing the original $P_{Trc2}$ promoter (Figure 2C), ones containing the $P_{T3}$ promoter achieved bistability across a wide range of expression variants (Figures 3D and S3B; Table S2), and long-term growth experiments confirmed that these toggles were bistable over 72 hr (Figure S3C). These experimental results confirm the mathematical analysis that decreased promoter leakage $\varepsilon$ would move the toggle switch toward bistability, yielding greater robustness to parameter variations (deterministic model, Supplemental Procedures 6) and greater robustness to noise (stochastic model, Figure S4 and Supplemental Procedures 7). Interestingly, the model also predicts that increased repressor expression does not always increase bistability (Supplemental Procedures 6), in agreement with experimental data in which increased LacI expression reduces circuit bistability when paired with low TetR expression (Figure 3D).
Genomic Integration of the Toggle Switch and Metabolic Load Analyses

Genomic integration allows removal of plasmid selection and replication systems that can place a high metabolic load on the host cell and contribute to horizontal gene transfer and the potential spread of antibiotic resistance (Bush and Fisher, 2011; Woodford et al., 2011). To determine if the single-copy toggle switch remained functional upon genomic integration, we tested toggle switch function and stability following integration in the lacZ locus in E. coli. As shown in Figure 3E, the integrated L6-P3T4 toggle maintained state stability for more than 72 hr without antibiotic selection, as did several other single-copy toggle variants (Figure S3D). Furthermore, flow cytometry analysis of these cell populations showed monomodal distributions of cells in each state, confirming the population-wide stability of the circuits. Interestingly, the integrated single-copy toggle exhibited a narrowed distribution of fluorescence reporter expression compared to the single-copy plasmid, resulting in a measurable increase in circuit stability (Figure 3E). This is likely due to nonsynchronized replication of the single-copy plasmid and the bacterial genome, a well-studied phenomenon that results in variable copy number of the plasmid in a subset of cells (Heimstetter et al., 1997).

As the field of synthetic biology moves from proof-of-concept construction to practical implementation, it is increasingly important to consider the physiological context of the engineered genetic circuits. To determine if the integrated toggle has a reduced physiological burden on the cell, we compared the growth profiles of cells containing the integrated L6-P3T4 toggle switch to cells containing the parental multi-copy toggle switch. In contrast to the multi-copy plasmid that caused a clear growth defect, cells containing the integrated toggle displayed an identical growth rate to cells without the plasmid (Figure 3F).

Genetic Kill Switches Using the Integrated Single-Copy Toggle

To demonstrate the stability and functionality of the genome-integrated toggle switch, we used the bistable toggle to develop a genetic kill switch in which toxin expression from the LacI+ state creates a “death” state that kills the cell and the TetR+ state provides a “survival” state in which the toxin is strongly repressed (Figure 4A). In this circuit design, cell viability provides a direct measure of circuit function, and the escapee rate provides a sensitive measure of circuit stability, as any leaky expression of toxins from the survival state provides a strong selective pressure for inactivating mutations (Chan et al., 2016). We cloned the DNA gyrase inhibitor CcdB (Smith and Maxwell, 2006) or the type II endonuclease EcoRI (Cheng et al., 1984), into the LacI+ state, and cells were exposed to IPTG to push them into the TetR+ survival state. Circuit bistability should allow these cells to remain viable following removal of IPTG, but ATc induction should push cells into the LacI+ death state where toxin expression causes cell death. As predicted, cells containing CcdB- or EcoRI-encoded toggle switches remained fully viable in the absence of IPTG (Figure 4B) but displayed a 4-log drop in viability within 2 hr after exposure to ATc (Figure 4C). To measure long-term circuit stability and robustness, we maintained the circuits in their survival state without inducer for 72 hr and periodically measured killing efficiency following ATc induction. The kill switches remained fully functional at each time point, displaying killing activity at 72 hr that was comparable with the killing activity at 0 hr (Figure 4C).

Concluding Remarks

In this case study for synthetic circuit development, we used rational design and empirical analysis to convert a multi-copy genetic toggle switch into a single-copy circuit that displays increased bistability and places minimal metabolic burden on the host cell. Deterministic and stochastic models and experimental tests revealed the importance of transcriptional leakage ε in low-copy number circuits, as reduced basal TetR transcription improved the circuit’s robustness to parameter variation and noise. Conversion of existing multi-copy circuits into single-copy genetic networks will enable their
integration into complex, multilayered systems with minimized effect on the host cell’s viability and metabolic capacity. Additionally, the empirical strategies we developed to improve gene expression and reduce transcriptional leakage provide valuable design criteria for single-copy circuit construction. Strong agreement between the mathematical theory and the empirical results suggests that this forward-engineering approach will aid the design and construction of single-copy, genome-integrated genetic circuits.

EXPERIMENTAL PROCEDURES

Media and Chemicals

Togglers were performed in M9 minimal media (Fisher Scientific; 6.8 g/L Na2HPO4, 3 g/L KH2PO4, 0.5 g/L NaCl, 1 g/L NH4Cl) with 5 g/L glucose (Sigma) and 5 g/L casamino acids (Sigma), using appropriate antibiotics and inducers at the following concentrations: ampicillin (50 μg/mL), chloramphenicol (10 μg/mL), kanamycin (50 μg/mL), IPTG (1 mM), ATc (50 ng/mL), and arabinose (1 mg/mL). Luria-Bertani (LB) media (Fisher Scientific; 10 g/L tryptone, 5 g/L yeast extract, 10 g/L NaCl) was used for cell growth of E. coli cloning strains. All cloning was conducted using E. coli EPI3000 (Epicenter; F' mcrA Δ[lac prophA Δ(mrr-hsdRMS-mcrBC)Q80lacZ Δmfd]) and SM10 lacZΔM15 recA1 endA1 araD139 Δ(ara, leu)7897 galU galK (pTrc99A trcA dfr). E. coli MG1655 ΔlacI was used for all toggle tests and expression level quantification.

Cell Growth

Cells were inoculated from single colonies on LB agar plates and grown overnight in LB medium at 37°C and 300 rpm. Overnight cultures were diluted 200-fold into 96-well plates containing M9 medium as defined above with either IPTG or ATc and cultured for 12 hr at 37°C and 900 rpm. Cells were washed once with M9 media and then serially passaged in M9 media without IPTG or ATc by 200-fold dilution every 12 hr. Cell growth was monitored by measuring optical density at 600 nm (OD600), and all measurements were performed in 200 μl in 96-well, flat-bottom plates.

Single-Copy Plasmid Construction

All plasmids were constructed using established molecular cloning techniques (Maniatis et al., 1982) and Gibson assembly (Gibson et al., 2009). To construct the single-copy toggle switches, toggle elements in pKDL071 (Litcofsky et al., 2020) were inserted around the 5′ site and the insertion of five to ten random nucleotides was used to enhance LacI, TetR, GFP, and mCherry expression in the single-copy toggle switch. In particular, LacI expression was improved by modifying its PTrc2 promoter, the LacI-binding operator O1 was replaced by an Oid operator (metabolic engineers, 2016; 329–336, July 21, 2016) and the lacI locus according to previously described methods (Metcalf et al., 1996). The lacI site and the insertion of five to ten random nucleotides was used to enhance LacI, TetR, GFP, and mCherry expression in the single-copy toggle switch. In particular, LacI expression was improved by modifying its PTrc2 promoter, the LacI-binding operator O1 was replaced by an Oid operator (metabolic engineers, 2016; 329–336, July 21, 2016) and the lacI locus according to previously described methods (Metcalf et al., 1996).

Quantification of LacI and TetR In Vivo

C-terminal mCherry fusions to LacI and TetR were used to quantify LacI and TetR expression levels (pBAC-LC and pBAC-TC, respectively; GenBank accession numbers KT893256 and KT893257) (Chan et al., 2016). These backbone vectors were used to measure the expression of all LacI and TetR expression variants as listed in Table S3. A SpectraMax M5 microplate reader (Molecular Devices) was used to measure GFP and mCherry fluorescence with excitation/emission wavelengths of 488 nm/520 nm and 587 nm/610 nm and an emission filter cutoff at 515 nm and 610 nm, respectively.

Stability Tests Using Flow Cytometer Measurements

The fluorescence distribution of each sample was measured using a BD FACSaria flow cytometer (BD Biosciences). For all FACS samples, cells were fixed in PBS containing 2% paraformaldehyde before analysis. At least 30,000 events were collected for each measurement, and FlowJo (Treestar) was used for data analysis. Threshold values for GFP and mCherry were set then defined by calculating the percentage of cells with fluorescence values above the threshold value (Figure S1B).

RT-qPCR

To quantify basal tetR or lacI expression, we sampled cells in exponential growth (OD600 ~0.3) in the presence of IPTG or ATc. Cultures were stabilized with RNAGuard Bacteria Reagent (QIAGEN), and total RNA was extracted using RNeasy Mini Kit (QIAGEN). An RNase-free DNase Kit (QIAGEN) was used to prevent possible DNA contamination, and total RNA was quantified using an ND-1000 NanoDrop spectrophotometer. Standard PCR was conducted using qPCR primers to identify any DNA contamination in the RNA samples, and the RNA samples were stored at −80°C. CDNA was synthesized from RNA samples using a Superscript III First Strand Synthesis kit (Invitrogen) and stored at −20°C. qPCR primers were designed using Primer3Plus software (Untergasser et al., 2007; Vega et al., 2012), and qPCR reactions were prepared according to the manufacturer’s instructions (LightCycler 480 SYBR Green I Master Kit, Roche Applied Science). A qPCR reaction with cDNA was used as a negative control, and five concentrations of lacI and tetR cDNA synthesized through in vitro transcription were included for each primer set in all qPCR operations. In vitro transcription was performed according to the manufacturer’s instructions (MEGAScript T7 Transcription Kit, Ambion Inc). The in vitro transcription cassette containing T7 promoter was constructed in pECJ3 (Cameron and Collins, 2014) by inserting the T7 promoter upstream of tetR or lacI, and the transcription cassettes for tetR or lacI were then amplified by PCR with P1 and P2 primers as follows: P1-terR, AACAGTGCGCTGGCCGTCAC; P2-terR, TGTAGTCCTGCGACGTCGTCGAC; P1-lacI, TACAATGAGCCTGCTTAC; and P2-lacI, TCAATTTGTGCTCCAGAATGT. These amplified DNA fragments were used as templates for in vitro transcription. qPCR reactions with primers P3 and P4 were prepared as follows: preincubation (95°C for 5 min) and 45 cycles of three-stage amplification (95°C for 10 s, 58°C for 10 s, and 72°C for 10 s). The primer sequences for P3 and P4 are as follows: P3-terR, ATTTAGGTACCGGCTTAC; P4-terR, CCTGTAGTCCTGCTTAC; P3-lacI, GACATCCTGGAAGGTGATA; and P4-lacI, ACAAGTGGATGCCCCTCAC. After the thermal cycling reaction, a melting curve reaction (65°C ramped to 98°C, 10 s at each 1°C interval) was conducted to detect non-specific amplification or primer-dimer formation. To calculate the fg value per 1 ng total RNA, standard lacI and tetR cDNA from in vitro transcription (5,000, 1,000, 200, 40, 8, 1.6, and 1 fg RNA per reaction) were analyzed using Roche LightCycler 480 software with default parameters for absolute quantification analysis. qPCR was performed using four to six biological replicates for each reported measurement.

Genomic Integration

The conditional replicative plasmid pWM91 (Metcalf et al., 1996) was used for the genomic integration of the genetic toggle switches. This plasmid contains the R6K ori region, which only replicates in the presence of pir gene expression. E. coli SM1101 pir+ strain was used to replicate pWM91 and its derivatives. Toggle L1-P3 Tet (pBAC-L1-P3 Tet; GenBank accession number KX264179) was inserted into a pWM91 derivative containing homologous regions to lacZ (pWM91-L1-P3 Tet; GenBank accession number KX264180) and inserted into the lacZ locus according to previously described methods (Metcalf et al., 1996). Toggles L1-P3 Tet and L2-P3 Tet were inserted into the E. coli genome in the same manner using plasmids pWM91-L1-P3 Tet and pWM91-L2-P3 Tet, respectively. To integrate kill switch variants of the toggle switch into the
Cell viability was assayed by colony forming unit (CFU) measurement in LB medium. Samples were serially diluted in PBS over a 7-log range, and 5 μL of each dilution were spotted onto square Petri dishes containing LB agar (1.5% agar) and incubated overnight at 37°C. 

**Kill Switch Test**

Cells were grown overnight with IPTG and then transferred into fresh LB medium containing 50 ng/mL ATc to induce tetR expression. Samples were serially diluted in PBS over a 7-log range, and 5 μL of each dilution were spotted onto Petri dishes containing LB agar (1.5% agar) and incubated overnight at 37°C. Cell viability was measured by colony forming unit (CFU) measurement in LB medium. The survival ratio was calculated as follows: CFU/mL ATc-treated or post-IPTG)/(CFU/mL ATc-treated). 

**Mathematical Model**

Let L and T denote LacI and TetR, respectively. Furthermore, introduce pL and pT to denote the promoter of LacI and TetR, where cL and cT denote the repressed promoters of LacI and TetR by TetR and LacI, respectively, so that 

\[
\frac{dL}{dt} = p_L c_L + c_T p_T + M_L p_L c_L T + c_L p_L + M_T T
\]

where \(M_L = 4\) and \(M_T = 2\) (LacI and TetR form tetramers and dimers, respectively). Let \(p_L\) and \(q_L\) denote the production rate of LacI when its promoter is free of TetR and when it is repressed by TetR, respectively, so that 

\[
p_L = p_L + L\]

and 

\[
q_L = q_L / c_L
\]

Introduce \(a_T\) and \(q_T\) similarly for TetR, yielding 

\[
p_T = p_T + T\]

and 

\[
q_T = q_T / c_T
\]

Furthermore, define \(e_L = q_L / a_L\) so that it captures the leakiness of the LacI promoter if \(e_L = 0\) the promoter is tightly repressed by TetR, whereas \(e_L = 1\) corresponds to the case when TetR does not repress the production of LacI at all. Similarly, \(r_T = q_T / a_T\) captures the leakiness of the TetR promoter. Finally, let \(\delta_L\) and \(\delta_T\) denote the decay rates of LacI and TetR, respectively, so that 

\[
L \overset{\delta_L}{\rightarrow} 0 \quad \text{and} \quad T \overset{\delta_T}{\rightarrow} 0.
\]

To address robustness to noise, we consider a bistable toggle in one of the two stable equilibria, say the LacI+ state, so that the concentration of LacI increases as the concentration of TetR increases. 

The effects of the plasmid copy number \(n\) can be incorporated into the reaction parameters as \(p = n\beta_0\) and \(b = b_0 / n\) where \(\beta_0\) and \(b_0\) are fixed constants, and they denote the values of \(\beta\) and \(b\) in the single-copy plasmid case (\(n = 1\)). The resulting mathematical model and its analysis are detailed in the Supplemental Information.

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